Thermodynamics (MP460) Assignment 3

Please hand in your solutions no later than Monday, October 17, 10:05 am. Late assignments will not be accepted. If you have questions about this assignment, please ask your lecturer, Joost Slingerland, (joost-at-thphys-dot-nuim-dot-ie), Office 1.7D, Mathematical Physics

Ex. 3.1 and 3.2

Ex. 3.1 is exercise 2 on page 28 of the book by Fermi. Ex. 3.2 is exercise 3 on page 28 of the book by Fermi.

Ex. 3.3: Useful identities for derivatives

In this exercise, you will derive a number of identities for derivatives which are very useful in thermodynamic calculations. Let A, B and C be three thermodynamic variables related by a single equation of state, so that we can choose two of the variables as the independent variables and then the other will be a function of the first two. For example, we can choose A and B to be independent and then C = C(A, B) is a function of A and B, but we could also choose A and C or B and C as the independent variables. The canonical example would have A, B and C equal to the pressure, temperature and volume of a gas, but the equations below will work for any triple of quantities.

- a. We take A and B as independent quantities. In some process, these are varied by infinitesimal amounts dA and dB. Write an equation for dC in terms of dA, dB and derivatives of C(A, B).
- b. Derive the following three identities

$$\begin{pmatrix} \frac{\partial C}{\partial A} \end{pmatrix}_{B} \begin{pmatrix} \frac{\partial A}{\partial B} \end{pmatrix}_{C} + \begin{pmatrix} \frac{\partial C}{\partial B} \end{pmatrix}_{A} = 0 \\ \begin{pmatrix} \frac{\partial A}{\partial B} \end{pmatrix}_{C} \begin{pmatrix} \frac{\partial B}{\partial A} \end{pmatrix}_{C} = 1 \\ \begin{pmatrix} \frac{\partial A}{\partial B} \end{pmatrix}_{C} \begin{pmatrix} \frac{\partial B}{\partial C} \end{pmatrix}_{A} \begin{pmatrix} \frac{\partial C}{\partial A} \end{pmatrix}_{B} = -1$$

Hint: One way to do this is to use the result of part \mathbf{a} . for the case of a process in which C is constant.