

EE106 – Engineering Mathematics I

Problem Set 11

Due by 5pm on Friday, 21 December 2018

1. Find the mean value of the function

$$f(x) = 1 + x \sin(x)$$

over the interval $[\pi, 2\pi]$.

2. A decaying voltage has the form

$$V(t) = V_0 t e^{-2t}$$

where V_0 is a positive constant. Find the root-mean-squared (RMS) value of this voltage between $t = 0$ and $t = 1$.

3. Use Newton's method to obtain an estimate for the zero of the cubic function

$$f(x) = 4x^3 - 3x^2 + 2x - 1$$

by starting with an initial guess of $x_1 = 1$. Stop when you obtain two successive estimates that differ by less than 0.001. (You should get to this level of precision after only a few iterations.)

4. Simpson's rule says that if we choose to divide the interval $[a, b]$ into four regions, then

$$\int_a^b f(x) dx \approx \frac{\Delta x}{3} [f(x_1) + 4f(x_2) + 2f(x_3) + 4f(x_4) + f(x_5)]$$

where $x_1 = a$, $x_5 = b$ and

$$x_i = a + (i - 1)\Delta x, \quad \Delta x = \frac{b - a}{4}$$

Use this to estimate the integral

$$\int_1^2 \frac{1}{x^2} dx$$

and compare your result with the exact answer of 0.5; namely, is it a good approximation, is it too far off to be reliable or is it adequate but not great?